

Drugs

Witt

Grade: 95 (5 points for structure of answers to 1, 2, 3, and 4)

Approriate Introduction	Looks good.
Explanation of prednisone	Nicely done.
Biological half-life	Good here as well.
Answers to 1, 2, 3, and 4	I appreciate that you took the time to get the LaTeX commands for the lists of answers, but the project description was specific in saying that your answers to these questions should be in paragraph form and not simply listed like an ordinary homework problem.
Proper formatting	Bravo on using the list environments to detail your answers to the questions. Unfortunately, as I said above, the answers were to be given in paragraph form.

List of Comments

Prednisone Project

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1 Abstract

2 In this project we were asked to construct a recursive model for the amount of
3 a drug that is present in a patient's bloodstream after a certain amount of time
4 and under certain conditions. Specifically, we were asked to learn more about
5 the drug Prednisone.

6 Prednisone

7 Prednisone is a synthetic corticosteroid drug, meaning it is a steroid that
8 helps things like immune response, stress relief, and regulating inflammation.
9 Hence, Prednisone is used to treat certain inflammatory diseases, autoimmune
10 diseases, and some types of cancer.

11 Biological Half-life

12 An important factor in this project is the biological half-life. All drugs, in-
13 cluding Prednisone, have a biological half life. The biological half-life is the
14 point in time where half of the pharmacological activity of the original dose of
15 the drug has left the body through the kidneys and liver. For Prednisone, the
16 biological half-life is one hour.

17 Prednisone Instructions

18 From the project description: "Prednisone is often prescribed for acute
19 asthma attacks and suppresses the immune system. For 5 mg tablets, typi-
20 cal instructions are: 'Take 8 tablets the first day, 7 the second, and decrease by
21 one tablet each day until all tablets are gone.'"

22 Procedure/Questions

23 Below are the models for different scenarios/time-periods of Prednisone in the
24 body.

- 25 1. Write formulas involving x , for the amount of Prednisone in the body:
- 26 (a) 24 hours after taking the first dose (of 8 tablets), right before taking
- 27 the second dose (of 7 tablets).
- 28 i. The formula I used is $x(t) = A_{d_0}(0.5)^t$
- 29 A. A_{d_0} = amount of the dose of Prednisone (in mg)
- 30 B. t = time (in hours)
- 31 C. 0.5 = biological half-life
- 32 ii. So, $x(24) = 40(0.5)^{24} = \mathbf{2.384e^{-6}}$ mg of Prednisone

- 33 (b) Immediately after taking the second dose (of 7 tablets).
34 i. The formula I used is $A_{d_0} = A_{d-1_f} + 5(n - (d - 1))$
35 A. A_{d_0} = amount of Prednisone immediately after the d th dose
36 B. A_{d-1_f} = amount of Prednisone 24 hours after the last dose
37 (in mg)
38 C. n = starting number of tablets = 8 tablets
39 D. d = dose that the patient is on = 2
40 ii. So, $A_{d_0} = 2.384e^{-6} + 35 \text{ mg} = \mathbf{35.000002384 \text{ mg of Pred-}}$
41 **nisone**
42 (c) Immediately after taking the third dose (of 6 tablets).
43 i. The formula I used is $A_{d_0} = A_{d-1_f} + 5(n - (d - 1))$
44 A. A_{d_0} = amount of Prednisone immediately after the d th dose
45 B. A_{d-1_f} = amount of Prednisone 24 hours after the last dose
46 (in mg)
47 C. n = starting number of tablets = 8 tablets
48 D. d = dose that the patient is on = 3
49 ii. So, $A_{d_0} = 35.000002384(0.5)^{24} + 30 = 2.086e^{-6} + 30 = \mathbf{30.000002086}$
50 **mg of Prednisone**
51 (d) Immediately after taking the eighth dose (of 1 tablet).
52 • To solve this, we must solve for the amount of Prednisone imme-
53 diately after taking each dose. We can do this given the previous
54 formula $A_{d_0} = A_{d-1_f} + 5(n - (d - 1))$, where A_{d_0} = the amount of
55 Prednisone immediately after the d th dose, A_{d-1_f} = the amount
56 of Prednisone 24 hours after the last dose (in mg), n = the start-
57 ing number of tablets (8 tablets), and d = the dose that the
58 patient is on. To solve for A_{d-1_f} , we use the other previous
59 formula, $x(t) = A_{d_0}(0.5)^t$, where t = the time in hours.

- 60 i. A_{4_0} : $A_{3_f} + 5(8 - (4 - 1)) = 30.000002086(0.5)^{24} + 25 =$
61 $1.79e^{-6} + 25 = 25.00000179$ mg of Prednisone immediately
62 after taking the 4th dose
63
- 64 ii. A_{5_0} : $A_{4_f} + 5(8 - (5 - 1)) = 25.00000179(0.5)^{24} + 20 =$
65 $1.49e^{-6} + 20 = 20.00000149$ mg of Prednisone immediately
66 after taking the 5th dose
67
- 68 iii. A_{6_0} : $A_{5_f} + 5(8 - (6 - 1)) = 20.00000149(0.5)^{24} + 15 =$
69 $1.19e^{-6} + 15 = 15.00000119$ mg of Prednisone immediately
70 after taking the sixth dose
71

iv. A_{70} : $A_{6f} + 5(8 - (7 - 1)) = 15.00000119(0.5)^{24} + 10 = 8.94e^{-7} + 10 = 10.00000089$ mg of Prednisone immediately after taking the seventh dose

v. A_{80} : $A_{7f} + 5(8 - (8 - 1)) = 10.00000089(0.5)^{24} + 5 = 5.96e^{-7} + 5 = \mathbf{5.000000596}$ mg of Prednisone immediately after taking the eighth dose

(e) 24 hours after taking the eighth dose.

- Use this previous formula: $x(t) = A_{d_0}(0.5)^t$
 - i. A_{d_0} = amount of the dose of Prednisone (in mg)
 - A. In this case, the amount of Prednisone will be the amount in the system immediately after taking the eighth dose, or 5.000000596 mg of Prednisone.
 - ii. t = time (in hours)
 - iii. 0.5 = biological half-life
- $x(24) = 5.000000596(0.5)^{24} = \mathbf{2.98e^{-7}}$ mg of Prednisone

(f) n days after taking the eighth dose.

- Formula: $x(n) = \mathbf{5.000000596(0.5)^{24n}}$
- You can solve this using a process similar to part 1e). The only difference in the formula is using the variable n and making $t = 24$. n is a variable for the number of days passed. By doing this, you are solving for the number of days, but in hours. To convert to days, divide your final answer by 24.

2. If a patient takes all the Prednisone tablets as prescribed, how many days after taking the eighth dose is there less than 3% of a Prednisone tablet in the patient's body?

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• We know that one Prednisone tablet is 5 mg, so 3% of that tablet is $.03(5) = .15$ mg.

• We must set up an equation: $.15 \text{ mg} > 5.000000596(0.5)^{24n}$, where $n =$ the number of days.

(a) using a calculator, we find that **$n = .210787$ days or 5.059 hours.**

105 3. A patient is prescribed n tablets of Prednisone the first day, $n - 1$ the
 106 second, and one tablet fewer each day until all the tablets are gone. Write
 107 a formula that represents T_n , the number of Prednisone tablets in the
 108 body immediately after taking the final dose.

109 • To solve for this, I used formulas similar to the ones above:

(a)

$$A_{d_0} = A_{d-1_f} + 5(n - (d - 1))$$

(b)

$$T_n = \frac{A_{8_0}}{5}$$

(c)

$$T_n = \frac{5.000000596}{5} = 1.000000119$$

110 (d) **There are 1.000000119 tablets in the body immediately**
 111 **after taking the final dose.**

112 • Where A_{d_0} is the amount of Prednisone immediately after taking the
 113 d th dose, A_{d-1_f} is the amount of Prednisone 24 hours after the last
 114 dose (in mg), n is the starting amount of tablets (8), t is time in
 115 hours, and d is the dose that the patient is on. NOTE: You divide by
 116 5 because the formula models the mg of Prednisone in the body, not
 117 tablets. Dividing by 5 (mg) converts the model to number of tablets
 118 in the body.

119 4. If a patient accidentally takes all the Prednisone tablets at once, what
 120 percentage of a Prednisone tablet will be present in the patient's body?
 121 How long will it take for there to be less than 3% of a Prednisone tablet
 122 in the patient's body?

123 • If the patient takes all 36 Prednisone tablets at once, there are 180
 124 mg ($36 * 5$ mg), or 3600% of a Prednisone tablet in the body.

- 125 • To solve this, we must set up another equation: $180(0.5)^t = .15$ mg,
126 where t is the time in hours that it will take to be less than 3% of a
127 Prednisone tablet in the body.
128 (a) using a calculator, we find that **$n = 10.229$ hours.**

129 Conclusion

130 I enjoyed this project because the topic was very interesting to me. I had never
131 learned about modeling the amount of a drug in a human body at a point in
132 time, and doing this project made me realize how much has to be considered
133 when writing/administering the drug instructions. One still has to consider the
134 amount of the drug that is still in the body before taking another dose. This
135 concept confused me for quite some time and made writing the formulas much
136 harder. For example, question three was the hardest question for me. While
137 I believe I got the correct numerical answer, deriving a formula proved most
138 challenging, and I ended up deriving an extremely simple and minimal formula.
139 Otherwise, when I began to understand the concept, the rest of the project was
140 fairly straightforward. In addition, I found that writing many of these answers
141 in paragraph form was confusing and hard to follow, so I stuck to writing the
142 answers as a list, but with explanations integrated into the list.

143 Overall, I extremely enjoyed working on this project. This topic has been the
144 most interesting project topic so far, and it has also been the most challenging
145 project for me so far.